

Table of Integrals

1. $\int u \, dv = uv - \int v \, du$

11. $\int csc u \cot u \, du = -csc u + C$

2. $\int u^n \, du = \frac{u^{n+1}}{n+1} + C, \quad n \neq -1$

12. $\int \tan u \, du = \ln |\sec u| + C$

3. $\int \frac{du}{u} = \ln |u| + C$

13. $\int \cot u \, du = \ln |\sin u| + C$

4. $\int e^u \, du = e^u + C$

14. $\int \sec u \, du = \ln |\sec u + \tan u| + C$

5. $\int a^u \, du = \frac{a^u}{\ln a} + C$

15. $\int csc u \, du = \ln |csc u - \cot u| + C$

6. $\int \sin u \, du = -\cos u + C$

16. $\int \frac{du}{\sqrt{a^2-u^2}} = \sin^{-1} \frac{u}{a} + C$

7. $\int \cos u \, du = \sin u + C$

17. $\int \frac{du}{a^2+u^2} = \frac{1}{a} \tan^{-1} \frac{u}{a} + C$

8. $\int \sec^2 u \, du = \tan u + C$

18. $\int \frac{du}{u \sqrt{u^2-a^2}} = \frac{1}{a} \sec^{-1} \frac{u}{a} + C$

9. $\int \csc^2 u \, du = -\cot u + C$

19. $\int \frac{du}{a^2-u^2} = \frac{1}{2a} \ln \left| \frac{u+a}{u-a} \right| + C$

10. $\int \sec u \tan u \, du = \sec u + C$

20. $\int \frac{du}{u^2-a^2} = \frac{1}{2a} \ln \left| \frac{u-a}{u+a} \right| + C$

BASIC FORMS FORMS INVOLVING

$$\sqrt{a^2 + u^2}, a > 0$$

$$21. \int \sqrt{a^2 + u^2} du = \frac{u}{2} \sqrt{a^2 + u^2} + \frac{a^2}{2} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$22. \int u^2 \sqrt{a^2 + u^2} du = \frac{u}{8} (a^2 + 2u^2) \sqrt{a^2 + u^2} - \frac{a^4}{8} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$23. \int \frac{\sqrt{a^2 + u^2}}{u} du = \sqrt{a^2 + u^2} - a \ln \left| \frac{a + \sqrt{a^2 + u^2}}{u} \right| + C$$

$$24. \int \frac{\sqrt{a^2 + u^2}}{u^3} du = -\frac{\sqrt{a^2 + u^2}}{u} + \ln(u + \sqrt{a^2 + u^2}) + C$$

$$25. \int \frac{du}{\sqrt{a^2 + u^2}} = \ln(u + \sqrt{a^2 + u^2}) + C$$

$$26. \int \frac{u^2 du}{\sqrt{a^2 + u^2}} = \frac{u}{2} \sqrt{a^2 + u^2} - \frac{a^2}{2} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$27. \int \frac{du}{u \sqrt{a^2 + u^2}} = -\frac{1}{a} \ln \left| \frac{\sqrt{a^2 + u^2} + a}{u} \right| + C$$

$$28. \int \frac{du}{u^2 \sqrt{a^2 + u^2}} = -\frac{\sqrt{a^2 + u^2}}{a^2 u} + C$$

$$29. \int \frac{du}{(a^2 + u^2)^{\frac{3}{2}}} = \frac{u}{a^2 \sqrt{a^2 + u^2}} + C$$

FORMS INVOLVING

$$\sqrt{a^2 - u^2}, a > 0$$

$$30. \int \sqrt{a^2 - u^2} du = \frac{u}{2} \sqrt{a^2 - u^2} + \frac{a^2}{2} \sin^{-1} \frac{u}{a} + C$$

$$31. \int u^2 \sqrt{a^2 - u^2} du = \frac{u}{8} (2u^2 - a^2) \sqrt{a^2 - u^2} + \frac{a^4}{8} \sin^{-1} \frac{u}{a} + C$$

$$32. \int \frac{\sqrt{a^2 - u^2}}{u} du = \sqrt{a^2 - u^2} - a \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$$

$$33. \int \frac{\sqrt{a^2 - u^2}}{u^2} du = \frac{1}{u} \sqrt{a^2 - u^2} - \sin^{-1} \frac{u}{a} + C$$

$$34. \int \frac{u^2 du}{\sqrt{a^2 - u^2}} = -\frac{u}{2} \sqrt{a^2 - u^2} + \frac{a^2}{2} \sin^{-1} + C$$

$$35. \int \frac{du}{u \sqrt{a^2 - u^2}} = -\frac{1}{a} \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$$

$$36. \int \frac{du}{u^2 \sqrt{a^2 - u^2}} = -\frac{1}{a^2 u} \sqrt{a^2 - u^2} + C$$

$$37. \int (a^2 - u^2)^{\frac{3}{2}} du = -\frac{u}{8} (2u^2 - 5a^2) \sqrt{a^2 - u^2} + \frac{3a^4}{8} \sin^{-1} \frac{u}{a} + C$$

$$38. \int \frac{du}{(a^2 - u^2)^{\frac{3}{2}}} = \frac{u}{a^2 \sqrt{a^2 - u^2}} + C$$

FORMS INVOLVING $\sqrt{u^2 - a^2}$, $a > 0$

$$39. \int \sqrt{u^2 - a^2} du = \frac{u}{2} \sqrt{u^2 - a^2} - \frac{a^2}{2} \ln |u + \sqrt{u^2 - a^2}| + C$$

$$40. \int u^2 \sqrt{u^2 - a^2} du = \frac{u}{8} (2u^2 - a^2) \sqrt{u^2 - a^2} - \frac{a^4}{8} \ln |u + \sqrt{u^2 - a^2}| + C$$

$$41. \int \frac{\sqrt{u^2 - a^2}}{u} du = \sqrt{u^2 - a^2} - a \cos^{-1} \frac{a}{|u|} + C$$

$$42. \int \frac{\sqrt{u^2-a^2}}{u^2} du = -\frac{\sqrt{u^2-a^2}}{u} + \ln|u + \sqrt{u^2-a^2}| + C$$

$$43. \int \frac{du}{\sqrt{u^2-a^2}} = \ln|u + \sqrt{u^2-a^2}| + C$$

$$44. \int \frac{u^2 du}{\sqrt{u^2-a^2}} = \frac{u}{2}\sqrt{u^2-a^2} + \frac{a^2}{2} \ln|u + \sqrt{u^2-a^2}| + C$$

$$45. \int \frac{du}{u^2\sqrt{u^2-a^2}} = \frac{\sqrt{u^2-a^2}}{a^2 u} + C$$

$$46. \int \frac{du}{(u^2-a^2)^{\frac{3}{2}}} = -\frac{u}{a^2\sqrt{u^2-a^2}} + C$$

FORMS INVOLVING

$$a + bu$$

$$47. \int \frac{u \, du}{a+bu} = \frac{1}{b^2}(a + bu - a \ln|a + bu|) + C$$

$$48. \int \frac{u^2 \, du}{a+bu} = \frac{1}{2b^3}[(a + bu)^2 - 4a(a + bu) + 2a^2 \ln|a + bu|] + C$$

$$49. \int \frac{du}{u(a+bu)} = \frac{1}{a} \ln\left|\frac{u}{a+bu}\right| + C$$

$$50. \int \frac{du}{u^2(a+bu)} = -\frac{1}{au} + \frac{b}{a^2} \ln\left|\frac{a+bu}{u}\right| + C$$

$$51. \int \frac{u \, du}{(a+bu)^2} = \frac{a}{b^2(a+bu)} + \frac{1}{b^2} \ln|a + bu| + C$$

$$52. \int \frac{du}{u(a+bu)^2} = \frac{1}{a(a+bu)} - \frac{1}{a^2} \ln\left|\frac{a+bu}{u}\right| + C$$

$$53. \int \frac{u^2 \, du}{(a+bu)^2} = \frac{1}{b^3}(a + bu - \frac{a^2}{a+bu} - 2a \ln|a + bu|) + C$$

$$54. \int u \sqrt{a+bu} \, du = \frac{2}{15b^2}(3bu - 2a)(a + bu)^{\frac{3}{2}} + C$$

$$55. \int \frac{u \, du}{\sqrt{a+bu}} = \frac{2}{3b^2}(bu - 2a)\sqrt{a+bu} + C$$

$$56. \int \frac{u^2 \, du}{\sqrt{a+bu}} = \frac{2}{15b^3}(8a^2 + 3b^2u^2 - 4abu)\sqrt{a+bu} + C$$

$$57. \int \frac{du}{u\sqrt{a+bu}} = \frac{1}{\sqrt{a}} \ln\left|\frac{\sqrt{a+bu}-\sqrt{a}}{\sqrt{a+bu}+\sqrt{a}}\right| + C \quad \text{if } a > 0$$

$$= \frac{2}{\sqrt{-a}} \tan^{-1} \sqrt{\frac{a+bu}{-a}} + C \quad \text{if } a < 0$$

$$58. \int \frac{\sqrt{a+bu}}{u} \, du = 2\sqrt{a+bu} + a \int \frac{du}{u\sqrt{a+bu}}$$

$$59. \int \frac{\sqrt{a+bu}}{u^2} du = -\frac{\sqrt{a+bu}}{u} + \frac{b}{2} + \int \frac{du}{u\sqrt{a+bu}}$$

$$60. \int u^n \sqrt{a+bu} du = \frac{2}{b(2n+3)} [u^n(a+bu)^{\frac{3}{2}} - na \int u^{n-1} \sqrt{a+bu} du]$$

$$61. \int \frac{u^2 du}{\sqrt{a+bu}} = \frac{2u^n}{b(2n+1)} - \frac{2na}{b(2n+1)} \int \frac{u^{n-1} du}{\sqrt{a+bu}}$$

$$62. \int \frac{du}{u^n \sqrt{a+bu}} = \frac{\sqrt{a+bu}}{a(n-1)u^{n-1}} \int \frac{du}{u^{n-1} \sqrt{a+bu}}$$

TRIGONOMETRIC FORMS

$$63. \int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

$$64. \int \cos^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

$$65. \int \tan^2 u du = \tan u - u + C$$

$$66. \int \cot^2 u du = -\cot u - u + C$$

$$67. \int \sin^3 u du = -\frac{1}{3}(2 + \sin^2 u)\cos u + C$$

$$68. \int \cos^3 u du = \frac{1}{3}(2 + \cos^3 u)\sin u + C$$

$$69. \int \tan^3 u du = \frac{1}{2}\tan^2 u + \ln|\cos u| + C$$

$$70. \int \cot^3 u du = -\frac{1}{2}\cot^2 u - \ln|\sin u| + C$$

$$71. \int \sec^3 u du = \frac{1}{2}\sec u \tan u + \frac{1}{2}\ln|\sec u + \tan u| + C$$

$$72. \int \csc^3 u du = -\frac{1}{2}\csc u \cot u + \frac{1}{2}\ln|\csc u - \cot u| + C$$

$$73. \int \sin^3 u du = -\frac{1}{n}\sin^{n-1} u \cos u + \frac{n-1}{n} \int \sin^{n-2} u du$$

$$74. \int \cos^2 u du + \frac{1}{n}\cos^{n-1} u \sin u + \frac{n-1}{n} \int \cos^{n-2} u du$$

$$75. \int \tan^n u du = \frac{1}{n-1} \tan^{n-1} u - \int \tan^{n-2} u du$$

$$76. \int \cot^n u du = \frac{-1}{n-1} \cot^{n-1} u - \int \cot^{n-2} u du$$

$$77. \int \sec^n u du = \frac{1}{n-1} \tan u \sec^{n-1} u + \frac{n-2}{n-1} \int \sec^{n-2} u du$$

$$78. \int \csc^n u du = \frac{-1}{n-1} \cot u \csc^{n-2} u + \frac{n-2}{n-1} \int \csc^{n-2} u du$$

$$79. \int \sin a u \sin b u du = \frac{\sin(a-b)u}{2(a-b)} - \frac{\sin(a+b)u}{2(a+b)} + C$$

$$80. \int \cos a u \sin b u du = \frac{\sin(a-b)u}{2(a-b)} + \frac{\sin(a+b)u}{2(a+b)} + C$$

$$81. \int \sin a u \cos b u du = -\frac{\cos(a-b)u}{2(a-b)} - \frac{\cos(a+b)u}{2(a+b)} + C$$

$$82. \int u \sin u du = \sin u - u \cos u + C$$

$$83. \int u \cos u du = \cos u + u \sin u + C$$

$$84. \int u^n \sin u du = -u^2 \cos u + n \int u^{-1} \cos u du$$

$$85. \int u^n \cos u du = u^n \sin u - n \int u^{n-1} \sin u du$$

$$86. \int \sin^n u \cos^m u du = -\frac{\sin^{n-1} u \cos^{m+1} u}{n+m} + \frac{n-1}{n+m} \int \sin^{n-2} u \cos^m u du$$

$$= \frac{\sin^{n+1} u \cos^{m-1} u}{n+m} + \frac{m-1}{n+m} \int \sin^n u \cos^{m-2} u du$$

INVERSE TRIGONOMETRIC FORMS

$$87. \int \sin^{-1} u \, du = u \sin^{-1} u + \sqrt{1-u^2} + C$$

$$92. \int u \tan^{-1} u \, du = \frac{u^2+1}{2} \tan^{-1} u - \frac{u}{2} + C$$

$$88. \int \cos^{-1} u \, du = u \sin^{-1} u - \sqrt{1-u^2} + C$$

$$93. \int u^n \sin^{-1} u \, du = \frac{1}{n+1} [u^{n+1} \sin^{-1} u - \int \frac{u^{n+1} du}{\sqrt{1-u^2}}], \quad n \neq -1$$

$$89. \int \tan^{-1} u \, du = u \tan^{-1} u - \frac{1}{2} \ln(1+u^2) + C$$

$$94. \int u^n \cos^{-1} u \, du = \frac{1}{n+1} [u^{n+1} \cos^{-1} u + \int \frac{u^{n+1} du}{\sqrt{1-u^2}}], \quad n \neq -1$$

$$90. \int u \sin^{-1} u \, du = \frac{2u^2-1}{4} \sin^{-1} u + \frac{u\sqrt{1-u^2}}{4} + C$$

$$95. \int u^n \tan^{-1} u \, du = \frac{1}{n+1} [u^{n+1} \tan^{-1} u - \int \frac{u^{n+1} du}{1+u^2}], \quad n \neq -1$$

$$91. \int u \cos^{-1} u \, du = \frac{2u^2-1}{4} \cos^{-1} u - \frac{u\sqrt{1-u^2}}{4} + C$$

EXPONENTIAL LOGARITHMIC FORMS

$$96. \int ue^{au} \, du = \frac{1}{a^2}(au-1)e^{au} + C$$

$$100. \int \ln u \, du = u \ln u - u + C$$

$$97. \int u^n e^{au} \, du = \frac{1}{a} u^n e^{au} - \frac{n}{a} \int u^{n-1} e^{au} \, du$$

$$101. \int u^n \ln u \, du = \frac{u^{n+1}}{(n+1)^2} [(N+1)\ln u - 1] + C$$

$$98. \int e^{au} \sin bu \, du = \frac{e^{au}}{a^2+b^2} (a \sin bu - b \cos bu) + C$$

$$102. \int \frac{1}{uln u} \, dn = \ln |\ln u| + C$$

$$99. \int e^{au} \cos bu \, du = \frac{e^{au}}{a^2+b^2} (a \cos bu + b \sin bu) + C$$

HYPERBOLIC FORMS

$$103. \int \sinh u \, du = \cosh u + C$$

$$108. \int \operatorname{csch} u \, du = \ln |\tanh \frac{1}{2}u| + C$$

$$104. \int \cosh u \, du = \sinh u + C$$

$$109. \int \operatorname{sech}^2 u \, du = \tanh u + C$$

$$105. \int \tanh u \, du = \ln |\cosh u| + C$$

$$110. \int \operatorname{csch}^2 u \, du = -\coth u + C$$

$$106. \int \coth u \, du = \ln |\sinh u| + C$$

$$111. \int \operatorname{sech} u \tanh u \, du = -\operatorname{sech} u + C$$

$$107. \int \operatorname{sech} u \, du = \tan^{-1} |\sinh u| + C$$

$$112. \int \operatorname{csch} u \coth u \, du = -\operatorname{csch} u + C$$

FORMS INVOLVING

$$\sqrt{2au - u^2}, \quad a > 0$$

$$113. \int \sqrt{2au - u^2} du = \frac{u-a}{2} \sqrt{2au - u^2} + \frac{a^2}{2} \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$114. \int u \sqrt{2au - u^2} du = \frac{2u^2 - au^3 a^2}{6} \sqrt{2au - u^2} + \frac{a^3}{2} \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$115. \int \frac{\sqrt{2au - u^2}}{u} du = \sqrt{2au - u^2} + a \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$116. \int \frac{\sqrt{2au - u^2}}{u^2} du = \frac{2\sqrt{2au - u^2}}{u} - \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$117. \int \frac{du}{\sqrt{2au - u^2}} = \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$118. \int \frac{u \, du}{\sqrt{2au - u^2}} = -\sqrt{2au - u^2} + a \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$119. \int \frac{u^2 \, du}{\sqrt{2au - u^2}} = -\frac{(u+3a)}{2} \sqrt{2au - u^2} + \frac{3a^2}{2} \cos^{-1}\left(\frac{a-u}{a}\right) + C$$

$$120. \int \frac{du}{u \sqrt{2au - u^3}} = -\frac{\sqrt{2au - u^2}}{au} + C$$